

## SFB-Seminar Representation Stability (Teilprojekte C1 u. C3)

### ZEIT:

7.1.2014, 16:00 Uhr - 18:00 Uhr

### ORT:

Freie Universität Berlin  
Zuse-Institut, Hörsaal 2005 EG  
Takustraße 7  
14195 Berlin-Dahlem

### PROGRAMM:

16:00 - 16:45 **Prof. Benson Farb (University of Chicago)**

#### **Representation stability: a user's guide**

"Representation stability" refers to a phenomenon discovered a few years ago by Church-Farb that seems to occur all over mathematics; it was developed into a powerful theory with Ellenberg. One simple application gives results such as: the sequence of vector spaces  $V_n$  has dimension equal to a polynomial  $P(n)$  for  $n$  large enough. A common application is to the fixed degree (co)homology of a sequence of spaces  $X_n$ .

This has been applied to examples in algebraic topology (configuration spaces), algebraic geometry (moduli spaces of surfaces with  $n$  marked points, spaces of polynomials on rank varieties), number theory (cohomology of congruence subgroups), algebraic combinatorics (co-invariant algebras), and several other areas. In most cases nothing is known about the actual dimension of  $V_n$ , but this is now reduced in principle to a finite problem. The purpose of this talk will be explain to workers in different areas what this theory can do for them, and how they can apply it.

16:45 - 17:15 Kaffee-Pause

17:15 - 18:00 **Prof. Benson Farb (University of Chicago)**

#### **Kontakt:**

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## Representation stability in cohomology and asymptotics for families of varieties over finite fields

In this talk Prof. Benson Farb will consider two families  $X_n$  of varieties on which the symmetric group  $S_n$  acts: the configuration space of  $n$  points in  $\mathbb{C}$  and the space of  $n$  linearly independent lines in  $\mathbb{C}^n$ . He will explain via these two beautiful examples how non-experts can use the (twisted) Grothendieck-Lefschetz Fixed-Point Theorem in  $\ell$ -adic cohomology as a machine to convert information, as follows:

Input: How the multiplicity of a given irreducible representation  $V$  of  $S_n$  in  $H^*(X_n; \mathbb{Q})$  varies with  $n$

Output: Formulas for the number of polynomials over  $\mathbb{F}_q$  (resp. maximal tori in  $\mathrm{GL}_n(\mathbb{F}_q)$ ) with specified properties related to  $V$ .

In particular we explain how representation stability of  $H^*(X_n; \mathbb{Q})$  corresponds to asymptotic stability of various point counts as  $n \rightarrow \infty$ .

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